

3.1 Solve Linear Systems by Graphing

EXAMPLE 1 Solve a system graphically

Graph the linear system and estimate the solution. Then check the solution algebraically.

$$\begin{aligned}4x + y &= 8 \\2x - 3y &= 18\end{aligned}$$

$$4(3) + (-4) = 8$$

$$12 - 4 = 8$$

$$8 = 8$$

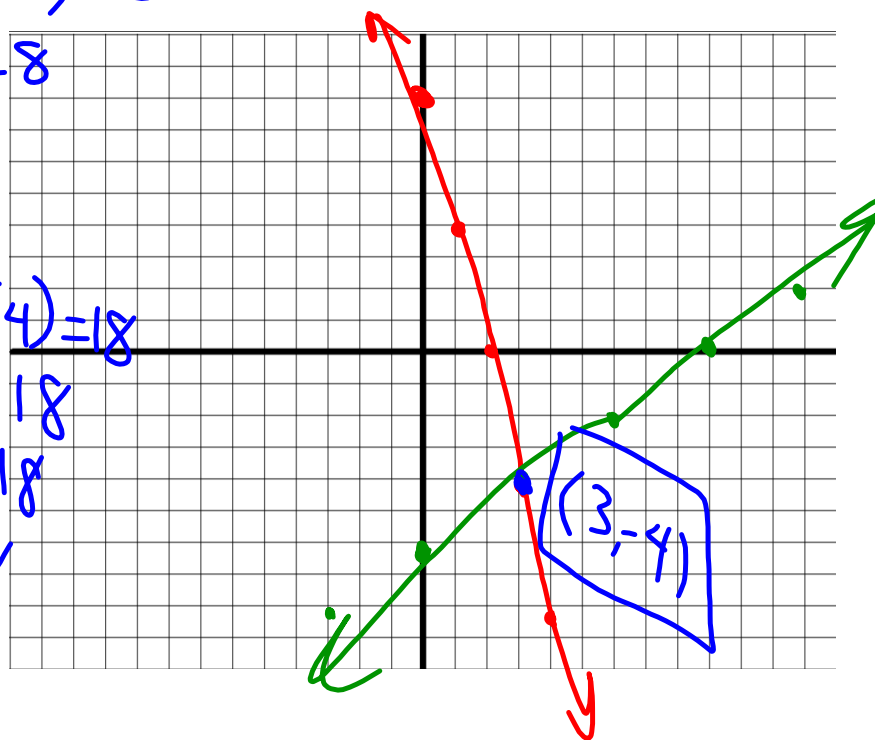
✓

$$2(3) - 3(-4) = 18$$

$$6 + 12 = 18$$

$$18 = 18$$

✓



EXAMPLE 1  **Solve a system graphically**

Graph the linear system and estimate the solution. Then check the solution algebraically.

$$3(-2) + 2(1) = -4$$

$$-6 + 2 = -4$$

$$-4 = -4$$

✓

$$(-2) + 3(1) = 1$$

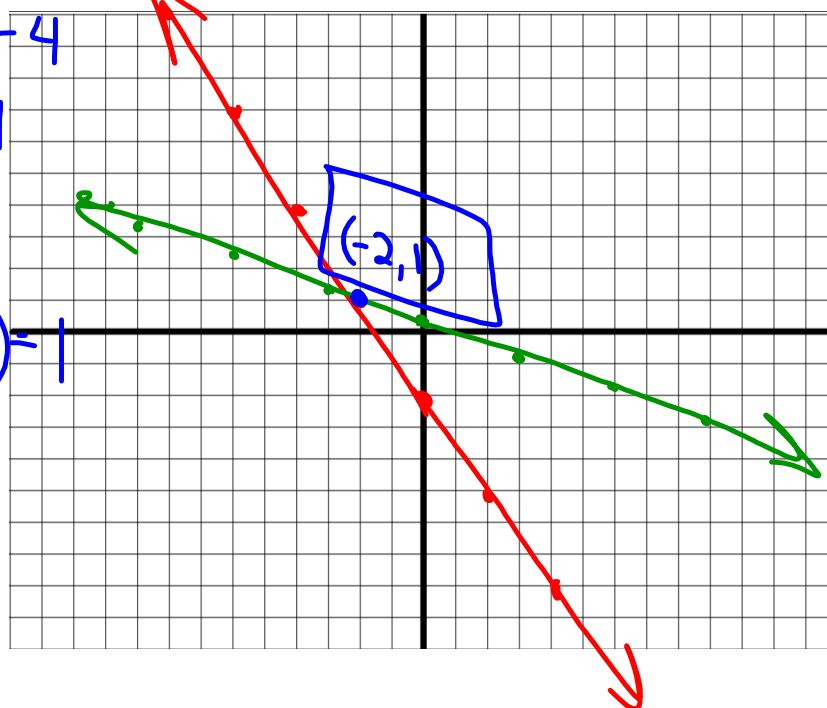
$$-2 + 3 = 1$$

$$1 = 1$$

✓

$$3x + 2y = -4$$

$$x + 3y = 1$$



Vocab:

Consistent- at least one solution

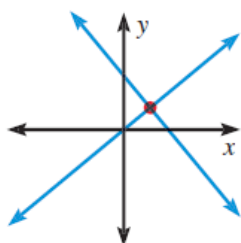
Inconsistent- no solution

Independent- exactly one solution

Dependent- many solution

Classify the systems as consistent/inconsistent and dependent/independent

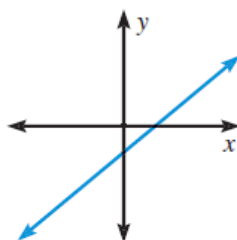
Exactly one solution



consistent

↓
independent

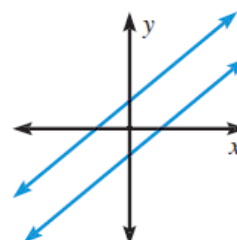
Infinitely many solutions



consistent

↓
dependent

No solution



inconsistent

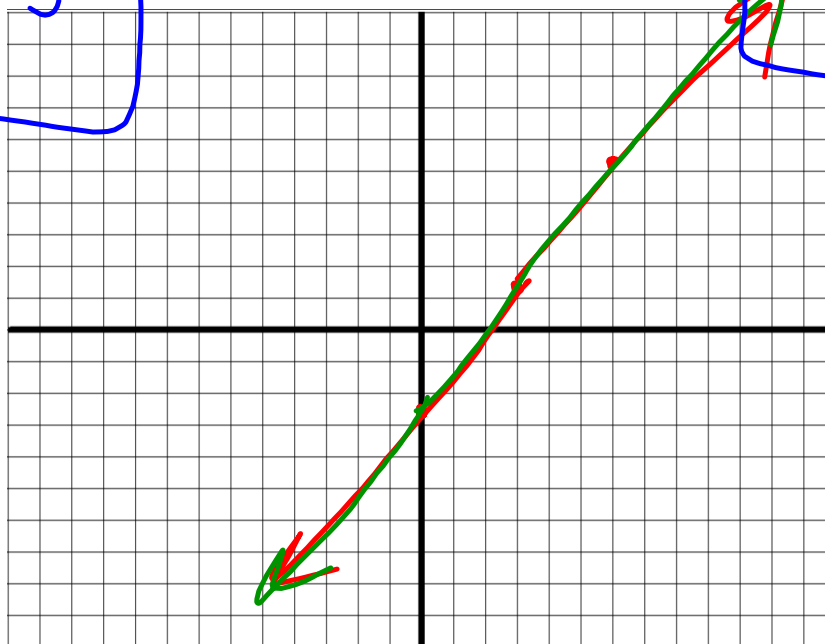
EXAMPLE 2 Solve a system graphically

Solve the system. Then classify the system as *consistent and independent*, *consistent and dependent*, or *inconsistent*.

$$\begin{aligned}4x - 3y &= 8 \\8x - 6y &= 16\end{aligned}$$

Infinitely many

class:
consistent & dependent



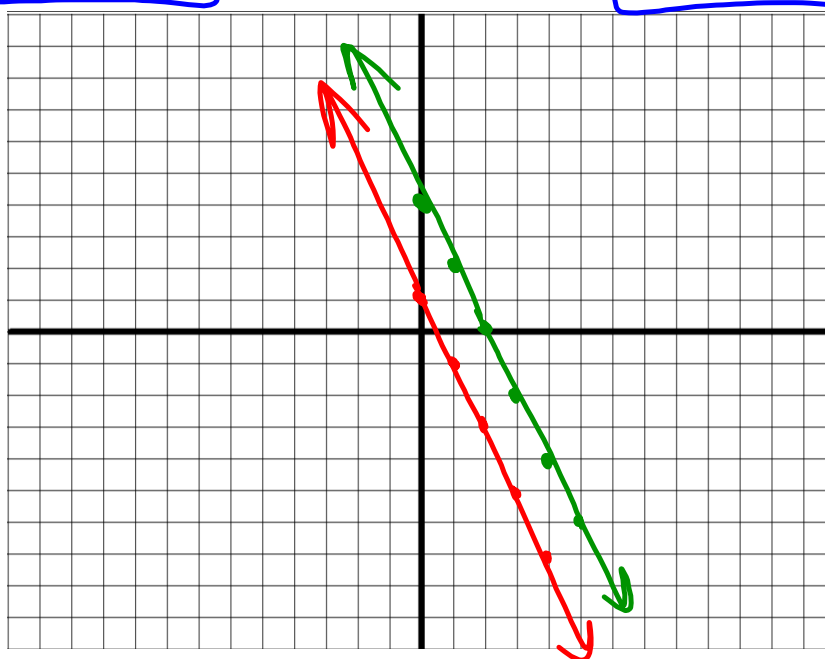
EXAMPLE 3 Solve a system graphically

Solve the system. Then classify the system as *consistent and independent*, *consistent and dependent*, or *inconsistent*.

no solution

$$2x + y = 4$$

$$2x + y = 1$$

class:
inconsistent

EXAMPLE 4

You ride an express bus from the center of town to your street. You have two payment options. Option A is to buy a monthly pass and pay \$1 per ride. Option B is to pay \$2.50 per ride. A monthly pass costs \$30. After how many rides will the total costs of the two options be the same?

Option A: $y = 30 + 1x$

Option B: $y = 0 + 2.5x$

