

## Answers for 5.7

For use with pages 383–386

### 5.7 Skill Practice

1. repeated

2. Complex conjugates include imaginary numbers and irrational conjugates include irrational numbers.

3. 4

4. 3

5. 6

6. 4

7. 7

8. 12

9. D

10.  $-1, 1, 2, 4$

11.  $-5, -3, 1, 2$

12.  $-2, 1, 3$

13.  $-5, -2, 2$

14.  $-1, 1, 4i, -4i$

15.  $-2, 1, 2i, -2i$

16.  $-3, -1, 2i, -2i$

17.  $-\sqrt{3}, -\frac{1}{2}, \sqrt{3}$

18.  $i, -i, 1 + \sqrt{3}, 1 - \sqrt{3}$

19.  $-4, -2, -\frac{3}{2}, 1$

20.  $f(x) = x^3 - 6x^2 + 11x - 6$

21.  $f(x) = x^3 - 2x^2 - 5x + 6$

22.  $f(x) = x^3 + 4x^2 - 7x - 10$

23.  $f(x) = x^3 - 4x^2 - 15x + 18$

24.  $f(x) = x^3 - 2x^2 + x - 2$

25.  $f(x) = x^4 - 4x^3 + 14x^2 - 36x + 45$

26.  $f(x) = x^4 - x^3 + 7x^2 - 9x - 18$

27.  $f(x) = x^4 - 18x^3 + 122x^2 - 370x + 425$

28.  $f(x) = x^3 - 4x^2 - 5x + 20$

29.  $f(x) = x^4 - x^3 - 18x^2 + 10x + 8$

30.  $f(x) = x^6 - 2x^5 - 18x^4 + 30x^3 + 89x^2 - 88x - 132$

31.  $f(x) = x^5 - 13x^4 + 60x^3 - 82x^2 - 144x + 360$

32. The conjugate of  $1 + i$ ,  $1 - i$ , must also be a zero;

$$\begin{aligned}f(x) &= (x - 2)[x - (1 + i)] \cdot \\&[x - (1 - i)] = (x - 2) \cdot \\&(x^2 - 2x + 2) = x^3 - 4x^2 + \\&6x - 4.\end{aligned}$$

33. Sample answer:

$$\begin{aligned}f(x) &= x^5 - 4x^4 + 6x^3 - \\&6x^2 + 5x - 2\end{aligned}$$

34. positive: 1, negative: 1, imaginary: 2

35. positive: 1, negative: 0, imaginary: 2

36. positive: 2 or 0, negative: 1, imaginary: 2 or 0

## Answers for 5.7 *continued*

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- 37.** positive: 2 or 0, negative: 3 or 1, imaginary: 4, 2, or 0
- 38.** positive: 3 or 1, negative: 2 or 0, imaginary: 4, 2, or 0
- 39.** positive: 3 or 1, negative: 2 or 0, imaginary: 4, 2, or 0
- 40.** positive: 3 or 1, negative: 3 or 1, imaginary: 4, 2, or 0
- 41.** positive: 2 or 0, negative: 1, imaginary: 6 or 4
- 42.**  $x \approx -2.7, x \approx 0.61, x \approx 3.1$
- 43.**  $x \approx -1.1, x \approx 1.3$
- 44.**  $x \approx -1.1$
- 45.**  $x \approx -0.58, x \approx 1.9$
- 46.**  $x \approx -1.4, x \approx 0.72, x = 1$
- 47.**  $x \approx -0.42, x \approx 2.0$
- 48.**  $x \approx -1.0, x \approx 1.0$
- 49.**  $x \approx -3.5, x \approx -1.1, x = -1, x \approx 2.1, x \approx 3.6$
- 50.** It cannot be imaginary because there are three total zeros and if one is imaginary, its conjugate also has to be a zero.
- 51.** There could be 3, 2, 1, or 0 positive zeros, 3, 2, 1, or 0 negative zeros, and 2 or 0 imaginary zeros.

**52.** C

**53.** Positive real zeros: 1, negative real zeros: 2, imaginary zeros: 0; the graph crosses the positive  $x$ -axis once and the negative  $x$ -axis twice.

**54.** Positive real zeros: 1, negative real zeros: 1, imaginary zeros: 2; the graph crosses the positive  $x$ -axis once and the negative  $x$ -axis once. Since the function has degree 4, the remaining 2 zeros must be imaginary.

**55.** Positive real zeros: 0, negative real zeros: 1, imaginary zeros: 4; the graph does not cross the positive  $x$ -axis and it crosses the negative  $x$ -axis once. Since the function has degree 5, the remaining 4 zeros must be imaginary.

**56.**  $f(2 - i) = (2 - i)^3 - 2(2 - i)^2 + 2(2 - i) + 5i =$   
 $2 - 11i - 6 + 8i +$   
 $4 - 2i + 5i = 0,$   
so  $2 - i$  is a zero;  
 $f(2 + i) = (2 + i)^3 - 2(2 + i)^2 +$   
 $2(2 + i) + 5i =$   
 $2 + 11i - 6 - 8i +$   
 $4 + 2i + 5i = 10i,$   
so  $2 + i$  is not a zero.

## Answers for 5.7 *continued*

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**57.**  $f(-1 + i) = (-1 + i)^3 + 2(-1 + i)^2 + 2i - 2 = 2 + 2i - 4i + 2i - 2 = 0$ ,  
so  $-1 + i$  is a zero;

$$\begin{aligned}f(-1 - i) &= (-1 - i)^3 + 2(-1 - i)^2 + 2i - 2 = \\&2 - 2i + 4i + \\&2i - 2 = 4i,\end{aligned}$$

so  $-1 - i$  is not a zero.

- 58.** The function is not a polynomial with real coefficients.

### 5.7 Problem Solving

**59.** year 3 and year 9

**60.** 1999

**61.** about 16.4 g per 100 mL

**62.** 1963

**63.** 0 in., about 59 in.; the bookshelf would have nearly 0 inches of deflection near each end because of the supports holding the bookshelf, so the answers make sense because they represent each end of a 60 inch bookshelf.



**64. a.** row 2:  $1000g, 1000g^2$ ;  
row 3:  $1000g$

**b.**  $v = 1000g^3 + 1000g^2 + 1000g + 1000$

**c.** About 1.048; about 4.8%; first I substituted \$4300 for  $v$  into the function in part (b) to get about 1.048. Then I subtracted 1 from the growth rate and changed it to a percent to find the interest rate.

**65.** about 4.3 ft

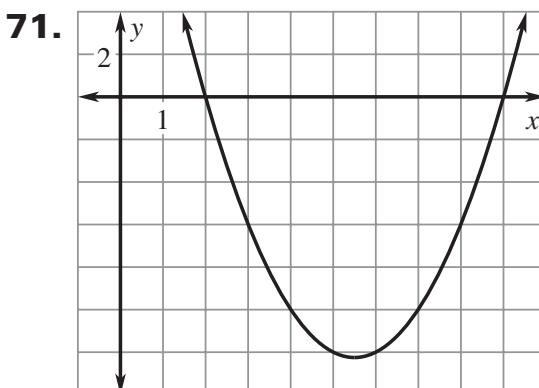
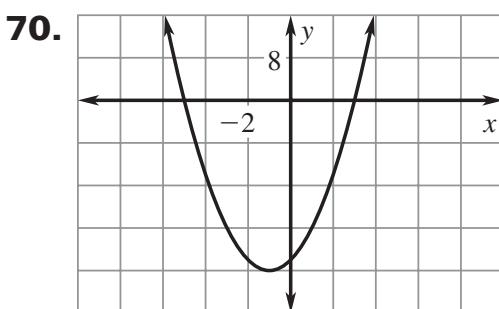
### 5.7 Mixed Review

**66.**  $-53$

**67.**  $-8$

**68.**  $-24$

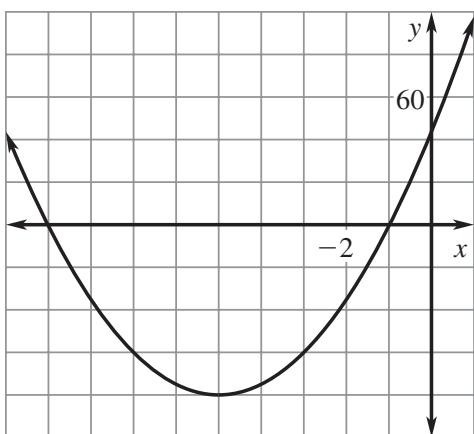
**69.**  $-18$



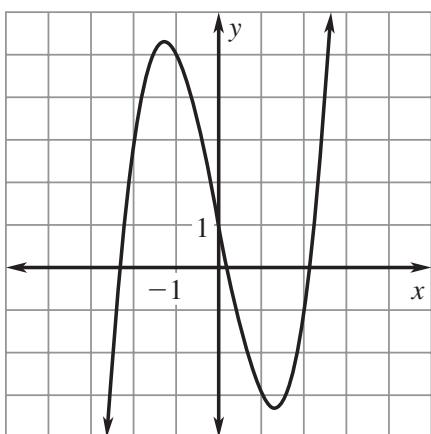
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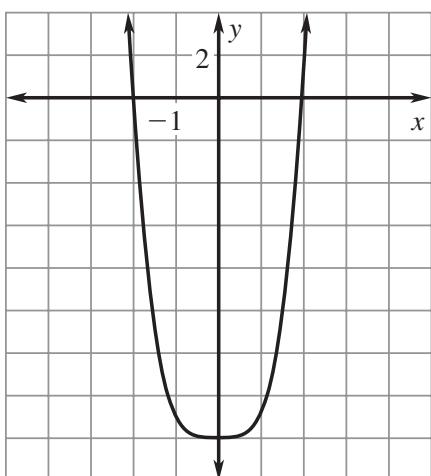
72.



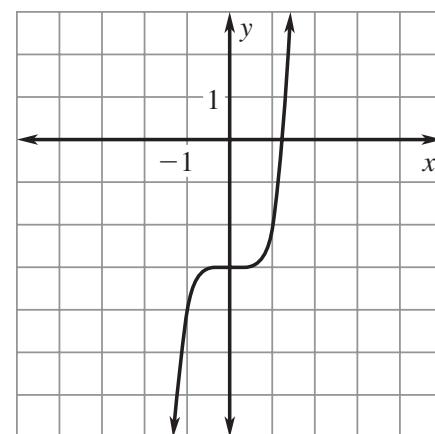
73.



74.



75.



76.  $y = \frac{1}{2}(x + 2)(x - 4)$

77.  $y = -2(x + 5)(x + 1)$

78.  $y = \frac{1}{3}(x - 2)(x - 7)$